Exercise 42

For the following exercises, find the inverse function. Then, graph the function and its inverse.

$$f(x) = \frac{3}{x - 2}$$

Solution

In order to find the inverse function, switch x with y in the given equation.

$$x = \frac{3}{y - 2}$$

Now solve for y.

$$x \times (y-2) = \frac{3}{y-2} \times (y-2)$$
$$xy - 2x = 3$$
$$xy = 3 + 2x$$
$$y = \frac{3+2x}{x}$$

Therefore, the inverse function is

$$f^{-1}(x) = \frac{3+2x}{x}.$$

